## Fast two-scale computational model for progressive damage analysis of fiber reinforced composites

Ibrahim Kaleel<sup>1</sup>, Marianna Maiarù<sup>2</sup>, Marco Petrolo<sup>1</sup>, Erasmo Carrera<sup>1</sup>, and Anthony M. Waas<sup>3</sup>

<sup>1</sup>Department of Mechanical and Aerospace Engineering, Politecnico di Torino,10129 Torino, Italy <sup>2</sup>Department of Mechanical Engineering, UMass Lowell, Lowell, MA 01854, USA <sup>3</sup>Department of Aeronautics and Astronautics, University of Washington, Seattle, WA 98195-2400, USA

## ABSTRACT

A fast two-scale finite element framework based on refined finite beam models for progressive damage analysis (PDA) of fiber reinforced composite is presented. The framework consists of a macro-scale model to define the structural-level components, interfaced with a second sub-scale model at the fiber-matrix level. Refined finite beam elements are based on Carrera Unified Formulation (CUF), a hierarchical formulation which offers a procedure to obtain refined structural theories that account for variable kinematic description [1]. The representative volume element (RVE) at the sub-scale is modeled with real material, e.g., fiber and matrix with details about packing and heterogeneity. Component-Wise approach (CW), an extension of refined beam kinematics based on Lagrange-type polynomials, is used to model the constituents in the sub-scale. Each consitutent in the sub-scale is modeled by the same finite element in the framework of the CW. The energy based crack band theory (CBT) is implemented within the sub-scale constitutive laws to predict the damage propagation in individual constituents [2, 3]. The communication between the two scales is achieved through exchange of strain, stress and stiffness tensor at every integration point in the macro-scale model. The efficiency of the framework is derived from the ability of CUF models to provide accurate displacement and stress fields at a reduced computational cost (approximately one order of magnitude of degrees of freedom less as compared to standard 3D brick elements). Numerical predictions are validated against the experimental results.

Keywords: Multiscale; CUF; Refined beam models; Progressive Damage Analysis; Crack Band

## References

- [1] Carrera E., Cinefra M., Petrolo M. and Zappino E., *Finite Element Analysis of Structures through Unified Formulation*, John Wiley and Sons, Ltd, 2014.
- Bažant Z. P. and Oh B. H., Crack band theory for fracture of concrete, Matériaux et Construction, 16:155-177,1983
- [3] Meyer P. and Waas A.M., Mesh-objective two-scale finite element analysis of damage and failure in ceramic matrix composites, 4:5, 2015